

# CH3771 Nuclear Chemistry Final Exam

(January 26, 2017)

- You will have 3 hours to complete this exam.
- Use of slides or book is not allowed
- Please add your name and student number on each sheet that you use and number the sheets
- Please do not use a pencil to write your answers
- You **MUST** show your work in order to receive any partial credit for incorrect answers.
- Composed by Antonia Denkova, Pablo Serra Crespo, Marcel Schouwenburg, and Elisabeth Oehlke

**GOOD LUCK!**

**Question 1**

To produce 2.5 kBq of <sup>241</sup>Am, 1 g of <sup>239</sup>Pu are irradiated for 30 days in a nuclear reactor ( $\phi=10^{15} \text{ cm}^{-2} \text{ s}^{-1}$ ).

- a) Write a scheme of all reactions and decays taking place, that are relevant for calculating the production yield of <sup>241</sup>Am. All data that you need is available in the nuclide chart shown below. The cross section for (n, $\gamma$ ) reactions is given as  $\sigma$ . The fission cross section is given as  $\sigma_f$ . (2 points)

<b>Cm 240</b> 27 d sf $\alpha$ 6.291; 6.248... sf g	<b>Cm 241</b> 32.8 d sf $\alpha$ 5.939... $\gamma$ 472; 431; 132... e <sup>-</sup> g	<b>Cm 242</b> 162.94 d sf $\alpha$ 6.113; 6.069... sf; g $\gamma$ (44...); e <sup>-</sup> $\sigma \sim 20$ $\sigma_f \sim 5$	<b>Cm 243</b> 29.1 a sf $\alpha$ 5.785; 5.742... e; sf; g $\gamma$ 278; 228; 210...; e <sup>-</sup> $\sigma$ 130; $\sigma_f$ 620	<b>Cm 244</b> 18.10 a sf $\alpha$ 5.805; 5.762... sf; g $\gamma$ (43...); e <sup>-</sup> $\sigma$ 15; $\sigma_f$ 1.1	<b>Cm 245</b> 8 a sf $\alpha$ 5... sf; g $\gamma$ 17... $\sigma$ 38	
<b>Am 239</b> 11.9 h sf $\alpha$ 5.774... $\gamma$ 278; 228... e <sup>-</sup> g	<b>Am 240</b> 50.8 h sf $\alpha$ 5.378... $\gamma$ 988; 889... g	<b>Am 241</b> 432.2 a sf $\alpha$ 5.486; 5.443... sf; $\gamma$ 60; 26... e <sup>-</sup> ; g; $\sigma$ 60 + 640 $\sigma_f$ 3.15	<b>Am 242</b> 141 a sf $\beta^-$ (49); e <sup>-</sup> $\alpha$ 5.206... sf; $\gamma$ (49...) $\sigma$ 1700 $\sigma_f$ 5900	<b>Am 242</b> 16 h sf $\beta^-$ 0.7; e <sup>-</sup> $\gamma$ (42...) e <sup>-</sup> ; g $\sigma$ 330 $\sigma_f$ 2100	<b>Am 243</b> 7370 a sf $\alpha$ 5.275; 5.233... sf; $\gamma$ 75; 44... $\sigma$ 75 + 5 $\sigma_f$ 0.079	<b>Am 244</b> 26 a sf $\beta^-$ 1... e <sup>-</sup> $\gamma$ (10...) e <sup>-</sup> ; g $\sigma_f$ 16
<b>Pu 238</b> 87.74 a sf $\alpha$ 5.499; 5.456... sf; Si; Mg $\gamma$ (43; 100...); e <sup>-</sup> $\sigma$ 510; $\sigma_f$ 17	<b>Pu 239</b> 2.411 · 10 <sup>4</sup> a sf $\alpha$ 5.157; 5.144... sf; $\gamma$ (52...) e <sup>-</sup> ; m $\sigma$ 270; $\sigma_f$ 752	<b>Pu 240</b> 6563 a sf $\alpha$ 5.168; 5.124... sf; $\gamma$ (45...) e <sup>-</sup> ; g $\sigma$ 290; $\sigma_f \sim 0.059$	<b>Pu 241</b> 14.35 a sf $\beta^-$ 0.02; g $\alpha$ 4.896... $\gamma$ (149...); e <sup>-</sup> $\sigma$ 370; $\sigma_f$ 1010	<b>Pu 242</b> 3.750 · 10 <sup>5</sup> a sf $\alpha$ 4.901; 4.856... sf; $\gamma$ (45...) e <sup>-</sup> ; g $\sigma$ 19; $\sigma_f < 0.2$	<b>Pu 243</b> 4 a sf $\beta^-$ 1... e <sup>-</sup> $\gamma$ 4... $\sigma$ 4	
<b>Np 237</b> 2.144 · 10 <sup>6</sup> a sf $\alpha$ 4.790; 4.774... $\gamma$ 29; 87...; e <sup>-</sup> $\sigma$ 170; $\sigma_f$ 0.020	<b>Np 238</b> 2.117 d sf $\beta^-$ 1.2... $\gamma$ 984; 1029; 1026; 924...; e <sup>-</sup> g; $\sigma_f$ 2600	<b>Np 239</b> 2.355 d sf $\beta^-$ 0.4; 0.7... $\gamma$ 106; 278; 228...; e <sup>-</sup> ; g $\sigma$ 32 + 19; $\sigma_f < 1$	<b>Np 240</b> 7.22 m sf $\beta^-$ 2.2... $\gamma$ 555; 597... e <sup>-</sup> hy...; g	<b>Np 240</b> 65 m sf $\beta^-$ 0.9 $\gamma$ 566; 974; 601; 448...; g	<b>Np 241</b> 13.9 m sf $\beta^-$ 1.3... $\gamma$ 175; (133...) g	<b>Np 242</b> 2.2 f sf $\beta^-$ 2.7... $\gamma$ 736; 780; 1473... g

- b) Write down the exact formula needed to calculate the production yield of <sup>241</sup>Am when irradiating <sup>239</sup>Pu with neutrons. To derive this you can use the general formula used for such calculations given below (not obligatory, you can also start from scratch). The final unit of the yield should be activity (Bq). (1 point)

$$N_n = C_1 e^{-\Lambda_1 t} + C_2 e^{-\Lambda_2 t} + \dots C_n e^{-\Lambda_n t}$$

$$C_1 = \frac{\Lambda_1^* \Lambda_2^* \dots \Lambda_{n-1}^*}{(\Lambda_2 - \Lambda_1)(\Lambda_3 - \Lambda_1) \dots (\Lambda_n - \Lambda_1)} N_1^0$$

$$C_2 = \frac{\Lambda_1^* \Lambda_2^* \dots \Lambda_{n-1}^*}{(\Lambda_1 - \Lambda_2)(\Lambda_3 - \Lambda_2) \dots (\Lambda_n - \Lambda_2)} N_1^0$$

$$\dots$$

$$C_n = \frac{\Lambda_1^* \Lambda_2^* \dots \Lambda_{n-1}^*}{(\Lambda_1 - \Lambda_n)(\Lambda_2 - \Lambda_n) \dots (\Lambda_{n-1} - \Lambda_n)} N_1^0$$

- c) Calculate or give the value of all constants (e.g.  $\Lambda_n$ ,  $\Lambda_n^*$ ,  $N_1^0$ ,  $t$ ,  $\lambda$ ) that are needed for the equation you have given in b). Give them in the units you would use for the calculation. (3 points)

**Question 2**

In 100g of a uranium containing mineral 0.06 cm<sup>3</sup> of Helium (at 0°C) were found. The uranium content of the mineral was 3 ppm. How old was the mineral? (<sup>238</sup>U, natural abundance 99.275%,  $t_{1/2}=4.468 \times 10^9$  a) (2 points)



**Question 3**

The radionuclide  $^{64}_{29}\text{Cu}$  is unstable ( $t_{1/2}=12.7\text{h}$ ).

- Which of the following 4 decays will it decay by: electron capture, beta minus emission, beta plus emission or alpha emission? For each decay type write the balanced equation. Given:  $m_n=1.008664$  amu,  $M_{\text{He}}= 4.002603$  amu,  $m_e= 5.485799 \times 10^{-4}$  amu and the table below. (3 points)
- What type of medical application can  $^{64}\text{Cu}$  be used for? (1 point)
- What other applications outside medicine are possible? (1 point)

Table B.1. Atomic mass tables (cont.)

N	Z	A	El	Atomic Mass ( $\mu\text{u}$ )	N	Z	A	El	Atomic Mass ( $\mu\text{u}$ )	N	Z	A	El	Atomic Mass ( $\mu\text{u}$ )
30	31		Ga	60 949170	40	27	Co	66 940610	38	34	Se	71 927112		
29	32		Ge	60 963790	39	28	Ni	66 931570	37	35	Br	71 936500		
28	33		As	60 980620	38	29	Cu	66 927750	36	36	Kr	71 941910		
39	23	62	V	61 973140	37	30	Zn	66 927130.9	35	37	Rb	71 959080		
38	24		Cr	61 955800	36	31	Ga	66 928204.9	45	28	73 Ni	72 946080		
37	25		Mn	61 947970	35	32	Ge	66 932738	44	29	Cu	72 936490		
36	26		Fe	61 936770	34	33	As	66 939190	43	30	Zn	72 929780		
35	27		Co	61 934054	33	34	Se	66 950090	42	31	Ga	72 925170		
34	28		Ni	61 928348.8	32	35	Br	66 964790	41	32	Ge	72 923459.4		
33	29		Cu	61 932587	42	26	68 Fe	67 952510	40	33	As	72 923825		
32	30		Zn	61 934334	41	27	Co	67 944360	39	34	Se	72 926767		
31	31		Ga	61 944180	40	28	Ni	67 931845	38	35	Br	72 931790		
30	32		Ge	61 954650	39	29	Cu	67 929640	37	36	Kr	72 938930		
29	33		As	61 973200	38	30	Zn	67 924847.6	36	37	Rb	72 950370		
40	23	63	V	62 976750	37	31	Ga	67 927983.5	35	38	Sr	72 965970		
39	24		Cr	62 961860	36	32	Ge	67 928097	46	28	74 Ni	73 947910		
38	25		Mn	62 949810	35	33	As	67 936790	45	29	Cu	73 940200		
37	26		Fe	62 940120	34	34	Se	67 941870	44	30	Zn	73 929460		
36	27		Co	62 933615	33	35	Br	67 958250	43	31	Ga	73 926940		
35	28		Ni	62 929672.9	43	26	69 Fe	68 957700	42	32	Ge	73 921178.2		
34	29		Cu	62 929601.1	42	27	Co	68 945200	41	33	As	73 923929.1		
33	30		Zn	62 933215.6	41	28	Ni	68 935180	40	34	Se	73 922476.6		
32	31		Ga	62 939140	40	29	Cu	68 929425	39	35	Br	73 929891		
31	32		Ge	62 949640	39	30	Zn	68 926553.5	38	36	Kr	73 933260		
30	33		As	62 963690	38	31	Ga	68 925581	37	37	Rb	73 944470		
40	24	64	Cr	63 964200	37	32	Ge	68 927972	36	38	Sr	73 956310		
39	25		Mn	63 953730	36	33	As	68 932280	47	28	75 Ni	74 952970		
38	26		Fe	63 940870	35	34	Se	68 939560	46	29	Cu	74 941700		
37	27		Co	63 935814	34	35	Br	68 950180	45	30	Zn	74 932940		
36	28		Ni	63 927969.6	33	36	Kr	68 965320	44	31	Ga	74 926501		
35	29		Cu	63 929767.9	43	27	70 Co	69 949810	43	32	Ge	74 922859.5		
34	30		Zn	63 929146.6	42	28	Ni	69 936140	42	33	As	74 921596.4		
33	31		Ga	63 936838	41	29	Cu	69 932409	41	34	Se	74 922523.6		
32	32		Ge	63 941570	40	30	Zn	69 925325	40	35	Br	74 925776		
31	33		As	63 957570	39	31	Ga	69 926028	39	36	Kr	74 931034		
41	24	65	Cr	64 970370	38	32	Ge	69 924250.4	38	37	Rb	74 938569		
40	25		Mn	64 956100	37	33	As	69 930930	37	38	Sr	74 949920		
39	26		Fe	64 944940	36	34	Se	69 933500	48	28	76 Ni	75 955330		
38	27		Co	64 936485	35	35	Br	69 944620	47	29	Cu	75 945990		
37	28		Ni	64 930088.0	34	36	Kr	69 956010	46	30	Zn	75 933390		
36	29		Cu	64 927793.7	44	27	71 Co	70 951730	45	31	Ga	75 928930		
35	30		Zn	64 929245.1	43	28	Ni	70 940000	44	32	Ge	75 921402.7		
34	31		Ga	64 932739.3	42	29	Cu	70 932620	43	33	As	75 922393.9		
33	32		Ge	64 939440	41	30	Zn	70 927727	42	34	Se	75 919214.1		
32	33		As	64 949480	40	31	Ga	70 924705.0	41	35	Br	75 924542		
31	34		Se	64 964660	39	32	Ge	70 924954.0	40	36	Kr	75 925948		
41	25	66	Mn	65 960820	38	33	As	70 927115	39	37	Rb	75 935071		

31 19	K	49 972780	36 19 55	K	54 999390	28 31	Ga	58 963370
30 20	Ca	49 957518	35 20	Ca	54 980550	27 32	Ge	58 981750
29 21	Sc	49 952187	34 21	Sc	54 967430	38 22 60	Ti	59 975640
28 22	Ti	49 944792.1	33 22	Ti	54 955120	37 23	V	59 964500
27 23	V	49 947162.8	32 23	V	54 947240	36 24	Cr	59 949730
26 24	Cr	49 946049.6	31 24	Cr	54 940844.2	35 25	Mn	59 943190
25 25	Mn	49 954244.0	30 25	Mn	54 938049.6	34 26	Fe	59 934077
24 26	Fe	49 962990	29 26	Fe	54 938298.0	33 27	Co	59 933822.2
23 27	Co	49 981540	28 27	Co	54 942003.1	32 28	Ni	59 930790.6
22 28	Ni	49 995930	27 28	Ni	54 951336	31 29	Cu	59 937368.1
34 17 51	Cl	51 013530	26 29	Cu	54 966050	30 30	Zn	59 941832
33 18	Ar	50 993240	25 30	Zn	54 983980	29 31	Ga	59 957060
32 19	K	50 976380	36 20 56	Ca	55 985790	28 32	Ge	59 970190
31 20	Ca	50 961470	35 21	Sc	55 972660	27 33	As	59 993130
30 21	Sc	50 953603	34 22	Ti	55 957990	39 22 61	Ti	60 982020
29 22	Ti	50 946616.0	33 23	V	55 950360	38 23	V	60 967410
28 23	V	50 943963.7	32 24	Cr	55 940645	37 24	Cr	60 954090
27 24	Cr	50 944771.8	31 25	Mn	55 938909.4	36 25	Mn	60 944460
26 25	Mn	50 948215.5	30 26	Fe	55 934942.1	35 26	Fe	60 936749
25 26	Fe	50 956825	29 27	Co	55 939843.9	34 27	Co	60 932479.4
24 27	Co	50 970720	28 28	Ni	55 942136	33 28	Ni	60 931060.4
23 28	Ni	50 987720	27 29	Cu	55 958560	32 29	Cu	60 933462.2
34 18 52	Ar	51 998170	26 30	Zn	55 972380	31 30	Zn	60 939514

#### Question 4

List 2 positive and 2 negative aspects of iNAA. (1 Point)

#### Question 5

In the last decade alpha radionuclide therapy is being used more and more in the fight against cancer.

- Explain from a biological point of view if alpha particles are suitable for cancer treatment (HINT: think of LET, tracks and kind of damage caused by alpha particles). Compare briefly with photon radiation. (2 points)
- Which alpha emitting radionuclide are most often used? (1 point)
- Explain what the recoil effect is and propose a possible solution (2 points)

#### Question 6

The Mossbauer effect is only possible when there is recoilless emission and absorption of a gamma photon.

- Calculate the recoil energy of a single  $^{57}\text{Fe}$  atom upon the emission of a gamma photon of 14.4 keV. (1 point)
- Based on the obtained result explain why the Mossbauer effect can only happen in solids. (Tip: The natural line width of the gamma emission is of the order of  $10^{-8}$  eV) (2 points)

#### Question 7

The hospital has decided to purchase a  $^{99}\text{Mo}/^{99\text{m}}\text{Tc}$  generator from a different supplier that claims that their generator is cheaper and better. Your boss has entrusted you, the nuclear chemist, with the task of checking the quality of the generator.

